## Entrance Examination for International Master's Program 2023

Departments of Mechanical Engineering and Hydrogen Energy Systems

## Fluids Engineering (Group A) [11:10~12:40]

## Question I

Water flows horizontally from left to right in a circular pipe as shown in the right figure. The diameter of the left part of the pipe is $D_{A}$. The pipe has a throat whose diameter is $D_{B}$ ( $D_{B}<$ $D_{A}$ ). When a small tube of negligible diameter containing different liquid is connected between the left part and the throat of the pipe, liquid shows the different height of $h$ between the left and right. The densities of water and liquid in the small tube, and the acceleration of gravity are denoted by $\rho, \rho_{m}$, and $g$, respectively $\left(\rho<\rho_{m}\right)$. The friction is assumed to be negligible, and the water flow is uniform at each cross-section of the pipe. Express the volumetric flow rate of water $Q$ by $D_{A}, D_{B}, h, \rho, \rho_{m}$, and $g$. ( 25 points)

## Question II

A circular water jet with the uniform velocity $V$ and the diameter $d$ impinges on a cone with the apex angle $\theta$ as shown in the figure. The axis of the jet is idenitical to the cone axis, and the flow around the cone is axi-symmetric and dettaches from the cone at the end. Assuming that the density of water is $\rho$, and the viscosity of water and the gravity are negligible, answer the following questions. ( 25 points)
(1) Find the force $F$ exerted by this jet on the cone when it is at rest.
(2) Find the force $F^{\prime}$ and the power $L$ exerted on this cone by the jet
 when it is moving with a velocity $u(<V)$ in the same direction as the jet.

